# Proof-of-Censorship: Enabling centralized censorship-resistant content providers

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**Abstract.** Content providers often face legal or economic pressures to censor or remove objectionable or infringing content they host. While decentralized providers can enable censorship-resistant storage, centralized content providers remain popular for performance and usability reasons. But centralized content providers can always choose not to respond to requests for a specific file, making it difficult to prevent censorship. If it is not possible to prevent, is it possible to detect and punish censorship on a centralized service?

A natural approach is to periodically audit the service provider by downloading the file. However, failure to download a file is not a proof of censorship. First, the provider could claim benign failure. Second, the proof is non-transferable: verifying censorship requires third parties to individually request the censored file. Moreover, a content provider may only selectively deny access to particular users or only for a short time frame. As such, checking by downloading does not work even for third parties who are online and willing to make queries.

In this paper, we introduce *proof of censorship*, whereby a content provider cannot delete or otherwise selectively remove content from their service without creating transferable cryptographic proof of their misdeed. Even if the provider restores the file at a later date, the proof remains valid, allowing the reputation of a content provider's commitment to censorship resistance to be based on the existence (or absence) of such proofs.

## 1 Introduction

Online censorship is done in many ways. In addition to blocking access to websites, censors also use legal means to remove information from content providers directly, such as through laws like the DMCA [5] in the United States. In the second half of 2016, Twitter received over 5,000 removal requests from government and police agencies worldwide, and complied with 19% of them [22]. In one example from August 2016, Twitter complied with a Brazilian government request to remove a tweet comparing then-mayoral candidate Rafael Greca to a fictional villain from the 1992 film Batman Returns [16].

This style of censorship can be significantly less apparent than overt website blocking. Because the service remains accessible, users are unaware of the content that may be secretly withheld from them. While some content providers (including Twitter) publish transparency reports containing overall statistics or examples of removed content [22, 7, 8], these reports are difficult to confirm or refute: How can users know if the transparency reports themselves have not been similarly censored?

While decentralized or distributed tools provide a way to make content robust against censorship, these techniques do not fully solve the problem. In a distributed censorship-resistant scheme, users must download and use specialized software which may itself be blocked by a censor. Due to this requirement, these tools are only utilized by well-informed users, while the majority of people rely exclusively on centralized content providers. Thus, there are clear advantages to providing censorship resistance in a centralized content storage context.

One idea proposed to incentivize censorship-resistant content providers to not delete data is to use *proof of retrievability* (PoR) to enable content providers to prove that they still retain a copy of a file. In PoR, providers respond to requests or challenges for specific subsets of a file they have agreed to store. A provider responds with the subset, proving (over many challenges) that they likely still store the entire contents of the file. With enough successful PoR challenge responses, a client can reconstruct the file, meaning that a provider that gives valid PoR responses for a file necessarily provides access to it. While this is a useful starting point, there are two major problems with this approach.

First, the content provider can always choose to not respond to a PoR request. Note that this is different from providing an invalid response to a request. By simply leaving a connection open and providing no response, the service never provides any incriminating evidence that they are not providing access to the file. While other clients can see this suspicious behavior, the provider could choose to respond correctly to some subset of users, seeding confusion and distrust over claims of censorship.

Second, the content provider can cease this behavior at any time, with no evidence that they ever censored a file. For example, a provider could wait until a certain number of users realized a file was removed or journalists started to ask questions before they reverted the decision to censor a file. Such a provider could pretend they never censored a file, and those that observed that they did would have no transferable proof. This allows a provider to censor files at will, and restore them only when convenient.

In this paper, we describe a way that a content provider can be held accountable for the files that they censor. We do this via a *proof of censorship* that a content provider unavoidably produces should they censor a file. Furthermore, these proofs are transferable, meaning that once one has been produced, others can verify the cryptographic proof and see that it attests to a censored file. Even if the content provider restores the original file, this proof still maintains the evidence of previous censorship.

To construct our proof of censorship, we use private information retrieval (PIR) which hides what information a client is requesting from a server. At a high level, servers commit to storing (encrypted) files by signing hashes of those files on upload. To download a file, a client performs a PIR query, which

the server responds to, signing both the PIR query and the server's response. Because the server does not know what file a client is requesting, it cannot selectively answer queries. To censor a file, the provider must return garbage data. Upon decryption of the PIR response, the client can confirm the file has been censored, and can reveal its PIR queries and the signed response to the world. Anyone with this proof (and the content provider's long-term public key) can verify that the content provider has removed the file.

Our proofs of censorship are compact and relatively efficient to verify: in the event of censorship, for a reasonable size database, the proof is on the order of a few megabytes, and takes approximately 50 milliseconds to verify on a laptop computer.



## 2 Background

**Fig. 1. Vector-Matrix PIR** — Private Information Retrieval involves a client making a query against a database. In Vector-Matrix PIR the client encrypts a vector of query elements and the server then multiplies the query elements against the database blocks homomorphically, using homomorphic addition to produce a single sum. This results in an encrypted value corresponding to the element where the client encrypted 1 (instead of 0), which is sent back to the client for decryption.

To describe our proof of censorship, we first provide background on private information retrieval (PIR) [13]. PIR allows a client to request data from a server without revealing to the server what data is being requested. A naive way to accomplish this is for the client to download the entire database from the server, then select its data locally. This method is bandwidth inefficient, however, and does not scale to large datasets.

There are two settings for PIR. In *information-theoretic* PIR (ITPIR), a set of N servers share the database, with clients making requests to all of them and combining their responses to obtain the requested files. If at least one of the servers is not colluding with the others, the client's request remains private. In *computational* PIR (CPIR), a single server stores the database, and clients use homomorphic-encrypted requests to retrieve data. As long as the computational hardness assumptions on the underlying cryptography hold, the server cannot determine what information the client requested. As we are focused on a single centralized content provider, in this paper, we only consider and describe CPIR.

Many CPIR schemes fall into the "matrix-vector" model [10], which is illustrated in Figure 1. In this model, CPIR uses a (IND-CPA-Secure, additive) homomorphic encryption that allows operations done on ciphertext to correspond to operations done on the corresponding plaintext. As an example, consider an additively homomorphic encryption function E() with corresponding decryption function D() that allows addition of ciphertext and multiplication by a constant; i.e,:

and

$$D(E(a) + E(b)) = a + b$$

$$D(E(a) \cdot c) = a \cdot c.$$

To perform a PIR query, a client constructs a vector of encrypted 0s and 1s. For example, if the server has n blocks, and the client wishes to retrieve block x from the server where  $0 \le x < n$ , the client sends a query vector Q to the server, comprised of  $q_{i\neq x} = E(0)$ , and  $q_x = E(1)$ . Note that the IND-CPA security of the encryption scheme implies that the server cannot determine which  $q_i$  is the encryption of 1.

With Q, the server (homomorphically) multiplies each  $q_i$  with its corresponding data block  $d_i$  in the database. The server then takes the homomorphic sum over the result. When  $i \neq x$ , the multiplication by E(0) will ensure the corresponding block does not contribute to the later-decrypted sum. The response is sent back to and decrypted by the client, resulting in  $D(\sum_i q_i \cdot d_i) =$  $D(E(1) \cdot d_x) = 1 \cdot d_x$ .

The PIR library that we use (XPIR [2]) provides two optimizations: recursion and aggregation. Recursion allows clients to send fewer query elements to the server, by breaking the database into a *d*-dimensional cube, and having the query select the row/column vectors. For example with a database of 100 records, it can be broken into a  $10 \times 10$  table of elements. The client sends 10 queries, which the server copies and applies to each row effectively selecting a singular column. Then, a separate 10 queries can be used to select a single element from that column. Thus the client sends a total of 20 query elements, as opposed to 100 (with no recursion).

Aggregation allows a client and server to pack multiple plaintext files into a single element. For example, if the ciphertext allows for an absorption of 768 bytes, but files are only 128 bytes, the database could utilize aggregation, fitting 6 files into each block. Clients then select the block of 6 files that contains their requested file, and locally discard the other 5. With aggregation, the client sends fewer request elements to the server, resulting in smaller queries.

## 3 Threat model

We consider a setting consisting of a single centralized content provider with multiple clients who upload and download content. Clients upload files to the provider, and distribute tickets that enable others to download the file. The information in a ticket can be summarized in a URL to be provided to others. This allows clients to easily share tickets in the same way they would distribute online content to others. In this model, we wish to detect a censoring content provider while preventing malicious clients from making false accusations. We achieve two properties:

- **Non-repudiation of targeted censorship** A provider cannot selectively censor a file while responding to queries from honest clients without producing a transferable proof of their misdeed.
- **Unforgeability** Against a non-censoring content provider, an attacker cannot forge a proof that a file was censored.

We note that our threat model does not prohibit a provider that chooses to delete or remove access to all of its files: a provider can always shut down entirely, or refuse to sign statements with its private key.

## 4 System design

In this section, we describe the details of our proof of censorship. A proof of censorship has two parts: a commitment from the server that it will store and distribute a file, and second, a later proof that it failed to uphold that commitment. The first part is obtained during file upload, where the server returns a signed and timestamped *ticket* that efficiently represents the commitment to store the file, while the second part is obtained when a client downloads the file the server is attempting to censor. We assume the server has a widely published long-term public signing key.

We begin our description assuming that a file fits in a single block that can be requested in a single PIR query to the server. In Section 4.2, we describe how to efficiently extend this idea to provide proofs of censorship for files that span multiple blocks.

#### 4.1 Proof of censorship construction

Ticket construction On upload, a client will upload an encrypted block that represents the file. The server chooses an index for the block to be stored, and provides a signature over the data and the index. For block data  $B_i$  stored at index *i*, the server hashes the block data to obtain  $H(B_i)$ . The server then signs the tuple containing a timestamp *t*, the index *i*, and the block hash  $H(B_i)$  using its long-term private key. This signature, along with *t*, *i*, and  $H(B_i)$  are sent to the client in the form of a *ticket*.

This ticket can be encoded into a URL that can be distributed easily to other users in the form of:

https://<service>/# $H(B_i)/i/t/sig$ 



**Fig. 2. Ticket creation** — When a file is uploaded, the server produces a signed ticket that commits the server to storing the block of data. The server signs a timestamp, the index where the data is stored, and a hash of the data, and returns this to the client for local storage.

where sig is the server's signature of the ticket. This gives the client all of the information it needs to verify as well as a simple way to distribute the ticket. Additionally the sensitive information is provided to the client in such a manner that it is not passed to the server, as values after a # symbol are only handled locally in browsers.

The client then verifies that the ticket is well formed and valid. First, the client hashes the data it has uploaded to obtain H(B). Then, it ensures that the timestamp t it received from the server is a recent timestamp<sup>3</sup>. Finally, the client checks the signature of the ticket, using t, i, and the client-computed H(B). If the signature is valid, the client stores the ticket for this block. If any checks fail, the client can attempt to re-upload their file until they receive a well-formed ticket. Figure 2 illustrates how tickets are generated during file upload.

File download To download a file, a client creates a PIR query that will result in a proof of censorship if it does not receive the file requested. During a normal PIR request, a client encrypts a vector of 0 and 1 elements using using random coins for the encryption. In our scheme, these coins are the output of a pseudorandom generator with a *seed* ( $Q_{seed}$ ) randomly selected by the client. This allows us to later reproduce the same query with only the seed and the index *i*. With this we create a compressed representation of the query which consists of the queried index (in the clear), and the seed.

The client creates the request Q and sends it to the server, along with the public key (as well as any cryptographic parameters needed to allow the server to

<sup>&</sup>lt;sup>3</sup> The client must ensure t is not located days in the future to avoid a server producing invalid proofs later.



**Fig. 3. Proof of censorship** — To verify a file is still in place, a client constructs a PIR query for its block. The server, without knowing which block was requested, signs the encrypted PIR query and the response it produces. The client decrypts the response, and can verify the data is correct. If it is not, the client can combine the signed response, the parameters it used to generate the PIR query, and the original ticket for this file to produce a stand-alone proof-of-censorship that can be verified by a third party.

perform homomorphic operations on the query<sup>4</sup>). The server then performs the query over its database using PIR, producing a short reply R that contains an encrypted representation of  $B_i$ . The server then hashes Q (including the public key) to obtain H(Q), and produces a signature over a timestamp t, the query hash H(Q), and the reply R. The server sends this signature, along with t and R to the client.

The client then extracts  $B_i$  from R using standard PIR extraction (i.e. decrypting R with its  $Q_{seed}$ -derived private key). The client then checks if this is the expected file by comparing it to the hash in the corresponding ticket for this file. If the client detects that the block has been censored, it now has a proof of censorship in the form of the server's response. The client publishes the original ticket, the server's signed PIR reply, and its  $Q_{seed}$  as a proof of censorship.

During this process, the server does not know what file is being requested. Therefore, to censor a file, the server must either not respond to any queries, or risk revealing that it has removed a file from its database.

*Verifying proofs of censorship* Given the server's public key, a signed ticket, a signed reply, and a query seed, a third party can verify whether the proof is valid evidence of censorship. To verify a proof of censorship, a verifier must perform several steps, detailed below.

<sup>&</sup>lt;sup>4</sup> E.g. in Paillier, this involves the public modulus generated by the client.

- 1. Check timestamps The verifier checks that the ticket's timestamp  $(t_t)$  is before the reply's timestamp  $(t_r)$ , ensuring that the query took place after the server committed to storing the file.
- 2. Check ticket signature Given the ticket's timestamp  $t_t$ , the requested index *i*, and the hash of the file  $H(B_i)$ , the verifier validates the ticket's signature with the server's public key.
- 3. Regenerate PIR query Verifier uses  $Q_{seed}$  and the index *i* to deterministically derive the PIR query Q, and computes the hash over the query H(Q).
- 4. Check reply signature Given the reply's timestamp  $t_r$ , the computed hash H(Q), and the server's reply, the verifier checks the reply's signature using the server's public key.
- 5. Extract reply Again using the key derived from  $Q_{seed}$ , the client extracts the PIR reply R to obtain  $B_i$ .
- 6. Check data hash The verifier finally compares the hash of the extracted data  $B_i$  to the hash committed to in the ticket. If the hashes are equal, the server did *not* censor the file, and returned the expected result. However, if the hashes do not match, this is a valid proof of censorship.

#### 4.2 Handling multiple blocks

So far, we have described how a client can efficiently receive a proof of censorship for a single uploaded block, but this does not address what happens if a file is larger than a single block. While a client could easily split up a file into multiple blocks, and receive a ticket for each block, storing each of these signed tickets may be expensive.

Instead, we can extend our design to allow for multiple blocks to receive a single ticket, while still allowing a proof to catch if an individual block is censored. To do this, our ticket will contain a Merkle tree root [18] in place of the single block's hash. The leaves of the Merkle tree will be the hashes of each block's data, and the ticket will consist of the list of hashes, and the final signature over the Merkle root, timestamp, and block index range.

To verify a proof, the verifier reconstructs the Merkle root from the suspected censored block and its Merkle tree-adjacent neighbors, and uses the root to verify the ticket. Thus, a verifier does not have to know all of the hashes of the tree, but rather only those that allow it to reconstruct the Merkle root (log(N)) hashes for an N-block file). This allows proofs to stay relatively compact even as the file size grows. After validation of the ticket, the verifier can be assured that the hash of the suspected block  $(H(B_i))$  they have been given is the correct hash for the given block  $B_i$ , and can perform the remaining checks described previously.

#### 4.3 Security argument

**Non-repudiation** We describe four basic ways a censoring server might attempt to behave in order to censor files while avoiding generating a proof of censorship. For these threats, we assume an honest client, that H is a collision

resistant hash function, and the query privacy of the PIR scheme. Our four scenarios enumerate the combination of if a server's strategy is to provide incorrect data vs. no data (or equivalently, forge signatures, as this will result in clients terminating), as well as if they they apply their strategy only to a specific set of files vs. indiscriminately. We model the server as a probabilistic polynomial-time algorithm.

- 1. Indiscriminate incorrect data In this scenario, the censoring server attempts to return incorrect responses to all queries. The server replaces all content  $B_i$  with  $B'_i$  indiscriminately, censoring all files. However due to the collision resistance of H,  $H(B_i) \neq H(B'_i)$  with all but negligible probability. Every client, upon receiving a response, will possess a valid proof-of-censorship that can be distributed.
- 2. Targeted incorrect data The server replaces only a specific (set of)  $B_i$  with  $B'_i$ , and responds honestly for all other files. As above, a client requesting file i will receive  $B'_i$  and, due to the collision resistance of H, will now possess a proof-of-censorship. In contrast to the indiscriminate case, this strategy only provides proofs of censorship for queries requesting file  $B_i$  in the set of censored files.
- 3. Indiscriminate non response The censoring server simply shuts down and responds to no queries. Proof-of-censorship cannot stop complete denial of services of this nature.
- 4. Targeted non response The censoring server attempts to not respond to queries for a specific file or files, while honestly responding to all others, thus not creating a proof for the censorship of the specific files. However, this is infeasible under our assumptions: Suppose a censoring server possesses such a capability. That is, assume the server has access to a probabilistic polynomial time (PPT) algorithm, A, that can decide whether it should respond to a given query q. With non-negligible advantage, for the targeted file A(q) should ideally return no response, while queries for other (non-censored) files, A(q) should respond with the correct data. In this case, the censoring server can construct a second PPT algorithm, B, that uses A as an oracle to distinguish between queries for a specific file vs. all other files. Thus, B succeeds in identifying queries for a specific file with the same non-negligible advantage as A. Since B would violate the query privacy of the PIR scheme, the algorithm A cannot exist.

**Unforgeability** We show that the scheme is unforgeable assuming the server's signature scheme is unforgeable, H is a random oracle, and the PIR scheme is the "vector-matrix type" [10] with an underlying homomorphic encryption scheme for which correctness holds with all but negligible probability.

Consider an attacker interacting with an honest content provider who produces a ticket and a forged proof of censorship for that ticket. Either the ticket or the PIR transcript (proof of censorship) must be forged. Forgeries in the ticket are prevented by the collision resistance of H and the security of the signature scheme. We now consider the case of forgeries in the PIR transcript. By the collision resistance of the hash function and security of the signature scheme, an attacker cannot substitute either the query or response. As such the PIR transcript itself must represent the actual query to and response from the provider. The only freedom an attacker has here is the choice of openings for the transcript (i.e. the random coins used for encryption and the public and private keys.), which she must reveal as part of the proof. Thus an attack must produce a correct looking query vector that when honestly combined with the database vector does not produce the correct result.

A homomorphic encryption scheme is said to be perfectly correct if for all choices of random coins, the operations  $gen, enc, dec, \cdot, +$  perform correctly. Perfect correctness nearly suffices to prevent an attacker from producing a purported query vector and ciphertext response that open to an invalid response.

However, there are two problems. First, correctness only holds with respect to the output of the algorithms. An attacker is not automatically bound to use the output of *gen* to make a key or *enc* to produce a ciphertext. If he does not use these algorithms, correctness makes no guarantees. A proof of censorship forces the attacker is to reveal their choice of random coins. This allows any verifier to check that a potential accuser did use *gen* and *enc* to produce keys and ciphertext for queries.

The second issue is that perfect correctness is a very strong property and does not hold for many cryptographic systems. Instead, correctness typically holds statistically. I.e when coins are chosen randomly, the probability of failure is negligible. This does not preclude an attacker from intentionally choosing such coins. To prevent this, we force coins to be selected as the output of a random oracle. I.e H(nonce|i) where i is the index to be queried and nonce is a randomly selected number.

As a result, an attacker who produces a forged transcript must have violated the correctness property of the encryption scheme underlying the PIR scheme (or successfully preimaged the secure hash function).

## 5 Implementation and Evaluation

We implemented our proof of censorship construction on top of XPIR, a fast PIR tool written in C++ [2]. Our implementation consisted of several hundred lines of modifications to XPIR, as well as an approximately 500-line application using the resulting libXPIR library. We used OpenSSL to perform the necessary signatures and hashes in our protocol.

The parameters we selected for testing were motivated by a simple textonly Twitter-like application, where messages are short (256 bytes, enough to include a short post and its metadata). We tested against a database of 1 million simulated messages in order to evaluate the time and size of different parts of the system. We used a quad-core Intel Core i5 CPU (3.30 GHz) with 32 GBytes of RAM to evaluate our prototype.

Table 1 shows the size and time to generate and validate our ticket, PIR query, and PIR reply (containing the proof). For our XPIR parameters, we

	Size	Generation time (std-dev)	Validation time (std-dev)
Ticket	120 bytes	334 $\mu$ s (0.53)	381 µs (4.61)
Query	3.8 Mbytes	28  ms (0.44)	n/a
$\operatorname{Reply}/\operatorname{Proof}$	2.0 Mbytes	2.8  s (0.19)	52  ms (0.54)

Table 1. Ticket and proof size — We implemented a prototype of our proof-ofcensorship system, simulating a database of 1 million 256-byte messages. We are able to keep a constant size of our proof at 2 MB. This allows clients that receive a proof of censorship to be able to easily distribute it.

choose to use XPIR's Learning with Errors implementation with 248 bits of security, using a polynomial of degree 2048 and a modulus of 60 bits, with recursion level (d) 3, and aggregation ( $\alpha$ ) 16. All of the client operations are relatively fast: ticket validation (395 µs), query generation (27 ms), plaintext extraction (3.5 ms), and proof validation (45 ms) suggest that clients could be implemented in smartphones or even Javascript web pages without significant performance issues [1].

#### 5.1 Scalability

We performed measurements of our proof of censorship and underlying PIR library to determine how the system scales. We measured the performance of downloading a single file with various database sizes, ranging from 5,000 to 1 million files of both small (256 byte) and large (1 MByte) size. For each database size, we used XPIR's built-in optimizer to determine the best parameters. XPIR chooses between two encryption options (Paillier, and the lattice-based learning with errors (LWE)), varying parameters of each to be optimal given a bandwidth estimate, file size, and number of files. We encouraged XPIR to optimize for small query and response sizes by providing a low bandwidth. Although Paillier produced the smallest query/responses, its server-side processing time was many orders of magnitude slower than LWE, effectively making it impractical. As a compromise between bandwidth and processing time, we selected LWE encryption optimized for small query and response sizes. For small files (256 bytes), the XPIR optimizer selected a polynomial of degree 2048 and 60-bit modulus with varying recursion and aggregation values depending on database size. When considering 1 MByte files the optimizer selected differing LWE flavors, all above the 80-bit security level, with polynomial degrees ranging from 2048 bits to 4096 bits and modulus bits ranging from 60 bits to 180 bits.

For each database size we measured the size of queries a client would have to generate and the time to generate them. On the server side we measured the amount of replies it needed to send (based on file size and aggregation value) and the time it took to construct those queries. And finally, back on the client side, we measured the time it took to extract the actual response from the given replies. The results of our experiments are shown in Tables 2, 3 and Figure 4.

For comparison, we allowed the optimizer to select Paillier 1024, which generates a 34.7 KB query and a 9.6 KB response when querying a 256 byte file

Number of files	5k	10k	50k	100k	500k	1M	10M	100M
Recursion depth	1	1	2	2	2	3	3	3
Aggregation value	300	420	96	64	126	16	16	15
Query size (MBytes)	0.53	0.75	1.44	2.5	3.9	3.8	8.0	17.7
Reply size (MBytes)	0.56	0.78	1.44	1.0	2.0	2.0	2.0	2.4
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**Table 2. Small file scaling**— We measured query and response sizes generated for several different database sizes with 256 byte files to determine how the system scales for a Twitter-like content server. We find that even at millions of files, the system remains relatively practical: an 8 MByte query and 2 MByte response are needed to select a single file privately (with accompanying proof of censorship) from 10 million files.

Number of files	5k	10k	50k	100k	500k	$1 \mathrm{M}$	10M	100M
Recursion depth	2	2	2	2	2	2	3	3
Aggregation value	1	1	1	1	1	1	1	1
Query size (MBytes)	17.8	25.0	14.0	19.8	44.2	62.5	121.3	174.1
Reply size (MBytes)	32.8	32.8	73.1	73.1	83.7	83.7	138.4	199.4

**Table 3. Large file scaling** — We also measured query and response sizes assuming 1 MByte files, to approximate our system being applied to an image or video-streaming content server. The XPIR optimizer chooses different security, polynomial and modulus parameters for each database size for 1 MByte files, due to it attempting to limit the amount of data the client has to send and receive over the network. While the parameters that are chosen are not always the most secure or privacy preserving, these parameters do result in the least amount of bandwidth necessary for clients to use. Additionally, while overheads are low, even with only 50 thousand files in a database, responses are 73 MBytes for a single megabyte file, likely making application of proof of censorship impractical to video streaming content providers.

from 1 million files. While this is several orders of magnitude smaller than LWE, server reply generation took nearly 2 hours for a single query. However, query generation and extraction times on the client were still fast (100ms and 77ms respectively). This suggests that with specialized modular arithmetic hardware on the centralized server, reply times could be considerably improved, potentially making this scheme practical and very attractive for its small query and response sizes.

We also note that a server need not contain all of its files in a single PIR database. Instead, one could partition the file space into many buckets, and requests could be made over a much smaller number of files in each bucket, similar to an idea proposed in bbPIR [25]. This allows for a tradeoff between the granularity at which a server can censor without producing a proof, and the efficiency or scalability of the system as a whole. With more buckets, a server could choose to not respond to queries for an entire bucket without producing a proof of censorship. If each bucket only contained a few files, the collateral damage to censoring the entire bucket could be small. In addition, if multiple buckets exist, a server that wishes to censor could place new files in their own



Fig. 4. Amount of time taken for the actions necessary for our tool to work. The time taken for the client to generate queries, and to extract the response from the server replies is very minimal compared to the amount of time that is spent by the server generating the replies to send back to the server. This time however can be decreased by using servers with hardware specifically designed to do these computations.

bucket, allowing for free censorship of the file in the future should it desire. To combat this, clients could choose which buckets they insert files into.

## 6 Discussion

In this section, we discuss possible attacks and defenses on our proof of censorship system, as well as describe potential incentives and future applications for this type of proof.

#### 6.1 Attacks

Server produces invalid tickets The server can choose to either not sign or not produce tickets during file upload, allowing it to delete those files later. However, the server does not know what file is being uploaded at the time of upload: the file could be encrypted, where the information to download the file (e.g. URL) contains the key used to decrypt it. Thus, the server must choose to produce tickets or not without knowing file contents, making it difficult to target specific content. In addition, clients that do not receive a valid ticket could reupload the file (perhaps through an anonymous proxy [6]) until they receive one.

Server doesn't sign replies By using PIR, the server does not know what file is being downloaded. Therefore, it cannot know if a particular request is for the file it wishes to censor. It can choose to never sign replies (or sign them randomly), but it does so without knowledge of the file involved. In this case, we can require that honest clients refuse to extract downloaded files unless the PIR reply contains a valid signature, meaning that the server effectively would be censoring unknown files that were requested. This is effectively the same as a server shutting down its service by not responding to any queries.

Incorrect timestamps A server can advance timestamps in tickets (or delay them in replies), tricking verifying clients into thinking a proof of censorship is invalid because the reply appears to come after the ticket (a feature used to protect against client forgeability). To solve this, we require clients to check the timestamps of tickets and replies and ensure they are recent before considering the response valid. This may still leave room for an equivocating server to leave a small window to censor a file, but if uploaded files are encrypted, the server will have little information to determine if the file should be censored before the window has passed.

#### 6.2 Incentives and Applications

How do we use a proof of censorship? The first answer is as a reputation sentinel: Proofs of censorship can be used to show others that a censoring content provider cannot be trusted. However, this only works if the proof is widely distributed (and not itself censored). As the proof is on the order of a few megabytes, it should be transferable to other verifiers via social media, email, or other contentsharing sites.

An intriguing possibility is to use proofs of censorship to impose a financial penalty. This could take the form of a smart contract in Ethereum [26] that controls a bond posted by the provider which is payable (in part) to whoever submits a valid proof of censorship.

Another option is to force the provider to reveal some sensitive secret if they ever censor a file. This can be accomplished via either multi party computation or trusted hardware. In either case, the content provider is forced to blindly interact with someone and evaluate a function that either returns nothing or, if fed a valid proof of work, returns the secret. For example, every request for a file could be accompanied by a query to the provider's SGX enclave [11] via an encrypted channel that is terminated within the enclave. The enclave could derive a private key from the secret loaded). If the enclave receives a valid proof of censorship, it returns the secret encrypted under the requester's key. Otherwise, it returns a dummy value. If the server chooses to provide no response at all, the honest client aborts.<sup>5</sup> This forces a censoring provider to either take down their whole system service once they have censored a file, or risk leaking their secret.

<sup>&</sup>lt;sup>5</sup> To prevent lazy but well meaning clients simply ignoring empty enclave responses, the enclave could instead return a decryption key needed for the particular file.

Proofs of censorship may also be purposefully created by a provider to disclose the extent of what they have censored. In an effort toward transparency, many content providers voluntarily report takedown notices and removal requests to Lumen [15] (formerly Chilling Effects). However, there is no guarantee that a provider hasn't withheld reports from this database. To combat this, providers could submit their own proofs of censorship to the database, and any proofs of censorship not present in the database serve as evidence of the provider attempting to secretly censor without reporting.

## 7 Related work

Previous research has explored alternative solutions to the problem of content censorship.

One such approach is proof of retrievability, proposed by Juels et al. in 2007 [12]. In this model, servers provide cryptographic proof to users that they have access to a file. However, as previously mentioned, this does not mean that a server must provide such a proof for every file requested: if the server knows what portion of a file is being requested, they can censor specific parts or files by simply not responding.

Several works have provided monetary incentives for successful proofs of retrievability. Permacoin proposes a cryptocurrency with proof of retrievability of an agreed-upon file in place of the traditional proof of work [19]. This encourages miners to keep portions of the file around in order to qualify for mining rewards associated with the currency. Lavinia incentivizes publishers to store documents by having a third-party verifier check and provide payments to well-behaved publishers in a distributed system [3].

Numerous projects have detailed the idea of combining files to discourage their removal from servers. Tangler [23] stores files across multiple servers and "entangles" newly uploaded files with existing files using Shamir secret sharing [20]. This entanglement means that deleting an old file may inadvertently remove more recently uploaded files that depend on it, increasing the collateral damage in censoring a file. Dagster [21] **xor**s blocks of data together requiring users to obtain multiple blocks from the server in order to retrieve one block of desired data. This combining of blocks ties files together in such a way that if older blocks are removed, newer blocks are no longer accessible. However, newly uploaded files are not protected, and access patterns of files could be used to detect what file is being downloaded.

Others have leveraged distributed systems to make content harder to censor. Publius [24] allows clients to upload encrypted files to multiple servers along with parts of a split encrypted key in such a way that a threshold of servers behaving honestly will allow the file to be retrievable. Freenet [4] provides a volunteer-based peer-to-peer network for file retrieval with the aim of allowing both authors and readers to remain anonymous. Tor [6] supports hidden services, where a central provider could potentially obscure its network location while hosting objectionable content. However, all of these schemes lack a mechanism to discourage servers or participants from misbehaving, opting instead to either hide or share responsibility of hosted content. Moreover, they provide no guarantees on file lifetimes, which is determined by the resource constraints of the participating servers.

# 8 Future Work

Proof of censorship could be extended in several directions and applications. As mentioned previously, monetary incentives built on top of such proofs could encourage content providers to deploy such a system and keep them honest.

Beyond this, there are many open problems in how to apply proof of censorship to different applications in an efficient manner. For instance, applying this scheme to a video streaming service would be a difficult engineering task, as large file sizes, database volumes, and high bandwidth demands require lowoverhead efficient solutions. To solve this problem, it may be possible to combine proof of censorship with other scalable private media retrieval systems such as Popcorn [9].

Proof of censorship could also augment existing key transparency applications, such as Certificate Transparency [14] or CONIKS [17]. Although these systems already detect server equivocation when a server modifies a particular object, they fail to provide any sort of guarantee on responses for every object in their certificate or key store. Using proof of censorship, these systems could provide such an assurance in addition to the protections provided.

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## 10 Conclusion

Content censorship from providers remains a growing problem. As network effects push users and content toward more centralized provider platforms, legal and political pressures have followed suit. While centralized providers can claim they stand for free speech or open access, they have no mechanism to prove they do.

In this paper, we have presented a scheme whereby a content provider can stand behind such a claim cryptographically. By deploying this scheme, providers will create a cryptographically verifiable and transferable proof of censorship should they delete or remove access to a specific file. The threat of this proof provides a disincentive to content providers from even temporarily censoring a file, as their reputation with respect to Internet freedom is at stake.

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